Definition 6.0.1. The statement $\lim_{n\to\infty} x = 0$ means that for any $\varepsilon > 0$, there is a number $N > 0$ for which $n \geq N$ implies $|x_n - 0| < \varepsilon$.