

Proof. To check that X is a solution to the SDE, it suffices to differentiate the RHS using Itô's formula (easier: compute $d(X_t Y_t)$). The uniqueness of solution can be deduced from Itô's Theorem (6.1.1). ■