Proof. Since (x_n) is a real sequence, $\inf \{ x \in S \}$ by hypothesis.