Definition 0.0.1. The statement $\lim_{n\to\infty} x_n = x$ means that for any real $\epsilon > 0$, there is a number $N > 0$ for which $n >= N$ implies $|x_n - x| < \epsilon$.