Definition 0.0.1. The statement $\lim_{x\to\infty} f(x) = L$ means that for any real $\epsilon > 0$, there is a number $N > 0$ for which $x > N$ implies $|f(x) - L| < \epsilon$.